

S.S.S. 2 FURTHER MATH HOLIDAY ASSIGNMENT

1. Find the equations of tangent and normal to the curve $x^2 + y^2 = 1$ at point $\left(1, \frac{\sqrt{3}}{2}\right)$.
2. If α and β are the roots of the equation $2x^2 - 7x + 4 = 0$, find the equation whose roots are $\frac{\alpha + 1}{\beta}$ and $\frac{\beta + 1}{\alpha}$.
3. The instantaneous displacement of a particle is given by $x = \ln \cos 2t - e^{\ln \sin t} + t$.
If $t = \pi$ seconds, find the exact values of its:
 - (a) displacement: x
 - (b) acceleration: $\frac{d^2x}{dt^2}$.
4. The position vector of a particle of mass $3Kg$ moving along a space curve at any time t seconds is given by $\mathbf{r} = (4t^3 - t^2)\mathbf{i} + (t - 2t^2)\mathbf{j}$; find the:
 - (a) velocity $\frac{d\mathbf{r}}{dt}$ of the body;
 - (b) acceleration $\frac{d^2\mathbf{r}}{dt^2}$ of the body;
 - (c) the magnitude of the force acting on the body $t = 2s$, correct to 4 sf.
5. The position vector of a body, with respect to the origin, is given by $\mathbf{r} = 4t\mathbf{i} + (12 - 3t^2)\mathbf{j}$ at any time t seconds. If $t = 1$ second, find, the:
 - (a) exact magnitude of the displacement of the body;
 - (b) velocity $\frac{d\mathbf{r}}{dt}$ of the body;
 - (c) exact magnitude of velocity of the body in its simplest form.